

## IONIC MIGRATION VELOCITY

**Attention! The text presented below is by no means enough to prepare for the practical.  
Please refer to recommended literature.**

Charged particle present in electric field experiences electric force  $F_{el}$  equal to:

$$F_{el} = qE, \quad (1)$$

where  $q$  refers to electrostatic charge value while  $E$  refers to intensity of electric field. When charged particles are ions, electrostatic charge value can be described by equation:

$$q = z \cdot e, \quad (2)$$

where  $z$  refers to ion valency while  $e$  refers to elementary charge. Relationship between intensity of electric field  $E$  and electric potential  $U$  can be presented as:

$$E = \frac{U}{d}, \quad (3)$$

where  $d$  refers to the distance between the point possessing potential  $U$  from the source of electric field. Electric force leads to accelerated motion of a charge in vacuum, while in non-vacuum media this motion is retarded by frictional force  $F_{op}$  proportional to the velocity of the charge (ion):

$$F_{op} = \mu \cdot v \quad (4)$$

For spherical objects having radius  $R$  and moving in a medium of viscosity  $\eta$  the proportionality factor  $\mu$  is equal to  $6\pi\eta R$ . Thus, the formula (4) can be rewritten into Stokes formula (Stokes law):

$$F_{op} = 6\pi\eta R \cdot v \quad (5)$$

According to first law of motion, an ion in solution moves with a constant speed  $v$  when  $F_{el} = F_{op}$ . Thus, the speed of ions in solution is proportional to the intensity of electric field  $E$ :

$$v = u \cdot E \quad (6)$$

In formula (6) the proportionality factor  $u$  is called ionic mobility (defined as a velocity at which ions move under the electric field intensity of  $1 \text{ V} \cdot \text{cm}^{-1}$ ). Since ionic mobility depends on solution concentration, it is useful to estimate ionic mobility for infinitely diluted solution ( $u_0$ ). Calculation of  $u_0$  allows for determination hydrodynamic radius  $R$  of an ion in solution. If an ion moves at constant speed when  $F_{el} = F_{op}$ , then

$$z \cdot e \cdot E = 6\pi\eta R \cdot v, \text{ and therefore } R = \frac{z e}{6\pi\eta u_0} \quad (7)$$

1. Velocity of an ion in solution  $v$  may be quantified by considering distance  $\Delta l$  travelled by the ion at constant speed versus time  $\Delta t$ .
2. Ionic mobility in solution may be calculated from the following formula:

$$u = \frac{\Delta l}{\Delta t} \frac{d}{U}, \quad (8)$$

where  $d$  refers to the distance between the electrodes,  $U$  refers to voltage applied to the electrodes.

3. Ionic mobility for infinite dilution ( $u_0$ ) may be found on the basis of the plot of ionic mobility ( $u$ ) versus solution concentration ( $c$ ) by extrapolation of the straight line to zero concentration.
4. Hydrodynamic radius of an ion ( $R$ ) can be calculated using formula (7).